

AOE 4134 Astromechanics  
Problem Sheet 1

Due September 4, 2002

Read Chapter 1 (Should be second reading. This time read it for understanding)

The following problems (1 - 7) deal with the following set of Vectors:

$$\vec{A} = 3\hat{i} + 2\hat{j} + 1\hat{k}$$

$$\vec{B} = 3\hat{i} - 5\hat{j} + 2\hat{k}$$

1. Determine  $|\vec{A}|$ ,  $|\vec{B}|$
2. Determine  $\vec{A} \cdot \vec{B}$
3. Determine  $\vec{A} \times \vec{B}$
4. Determine the angle between the two vectors
5. If  $\vec{B}$  is a position vector (units - meters) and  $\vec{A}$  is a force vector (units - Newtons), determine the moment (units - Newton meters) about the origin of the reference system.
6. Assuming the same vector designation as in prob. 5, determine the moment about the point  $(x,y,z) = (1,2,3)$ .
7. Find two points, other than the origin, that the moment of force ( $\vec{F} = \vec{A}$ ) equals zero.
8. The velocity at any point on a rotating body is given by  $\vec{V} = \vec{\omega}_{body} \times \vec{r}$ . Using the data from JGM-2, and assume a spherical earth, determine the magnitude of the velocity of someone
  - a) at sea level on the equator
  - b) in Blacksburg, altitude 2000 ft, and latitude of 37.229 degrees.
9. If  $r(t) = 5 \cos(3t)$  distance units, and  $\theta(t) = 2t^2$  Radians, find the position, velocity, and acceleration vectors when  $t = 3$  time units, that is find their radial and transverse components.
10. For the results in problem 9 find (at  $t = 3$  time units)
  - a) magnitude of  $\vec{r}$
  - b) magnitude of  $\dot{\vec{r}}$
  - c)  $\dot{r}$
  - d) magnitude of  $\ddot{\vec{r}}$
  - e)  $\ddot{r}$

