

Introduction to Attitude Dynamics and Control

Chris Hall
Aerospace and Ocean Engineering
cdhall@vt.edu

What is spacecraft attitude? And why should we care about it?

- Most spacecraft have instruments or antennas that must be pointed in specific directions
 - Hubble must point its main telescope
 - Communications satellites must point their antennas
- The orientation of the spacecraft in space is called its **attitude**
- To **control** the attitude, the spacecraft operators (which could be the spacecraft's computer in the case of an autonomous "ADCS") must have the ability to
 - Determine the current attitude
 - Determine the error between the current and desired attitudes
 - Apply torques to remove the error

Spacecraft Attitude Determination and Control

- So, the spacecraft needs an Attitude Determination and Control System (ADCS)
- To do the determination function requires knowledge of kinematics
- Attitude is determined using sensors
- To do the control function requires knowledge of kinetics and kinematics (dynamics)
- Attitude is controlled using actuators

Attitude Determination

Determine the **attitude**, or **orientation**, or **pointing direction** of a **reference frame** fixed in the **body**, with respect to a **known reference frame**, usually an inertial frame. That is, *where is the spacecraft pointing?*

- Generally involves finding a **rotation matrix**, or its equivalent
- Requires two or more **attitude sensors**
 - Sun sensor, Earth horizon sensor, Moon sensor, star tracker, magnetometer
- Requires an **algorithm**

The Differential Equation

- Every good dynamics course must begin with a differential equation
- For attitude dynamics and control, the equation of choice is

$$\dot{\vec{\mathbf{h}}} = \vec{\mathbf{g}} \quad \text{Euler (1707-1783)}$$

- This is the rotational equivalent of

$$m\vec{\mathbf{a}} = \vec{\mathbf{f}} \quad \text{or} \quad m\ddot{\vec{\mathbf{r}}} = \vec{\mathbf{f}} \quad \text{Newton (1643-1727)}$$

- Other notation used in other books and papers:

$$\dot{\vec{\mathbf{L}}} = \vec{\mathbf{N}} \quad \dot{\vec{\mathbf{H}}} = \vec{\mathbf{M}}$$

- *Why doesn't everybody get together and agree on a specific notation?*

Euler's Equations

- Euler's **vector** differential equation

$$\dot{\mathbf{h}} = \mathbf{g}$$

h is angular momentum
g is torque

- Becomes a **matrix** differential equation when expressed in a body-fixed reference frame

$$\mathbf{I}\dot{\boldsymbol{\omega}} = -\boldsymbol{\omega}^{\times}\mathbf{I}\boldsymbol{\omega} + \mathbf{g}$$

I is inertia matrix
 $\boldsymbol{\omega}$ is angular velocity

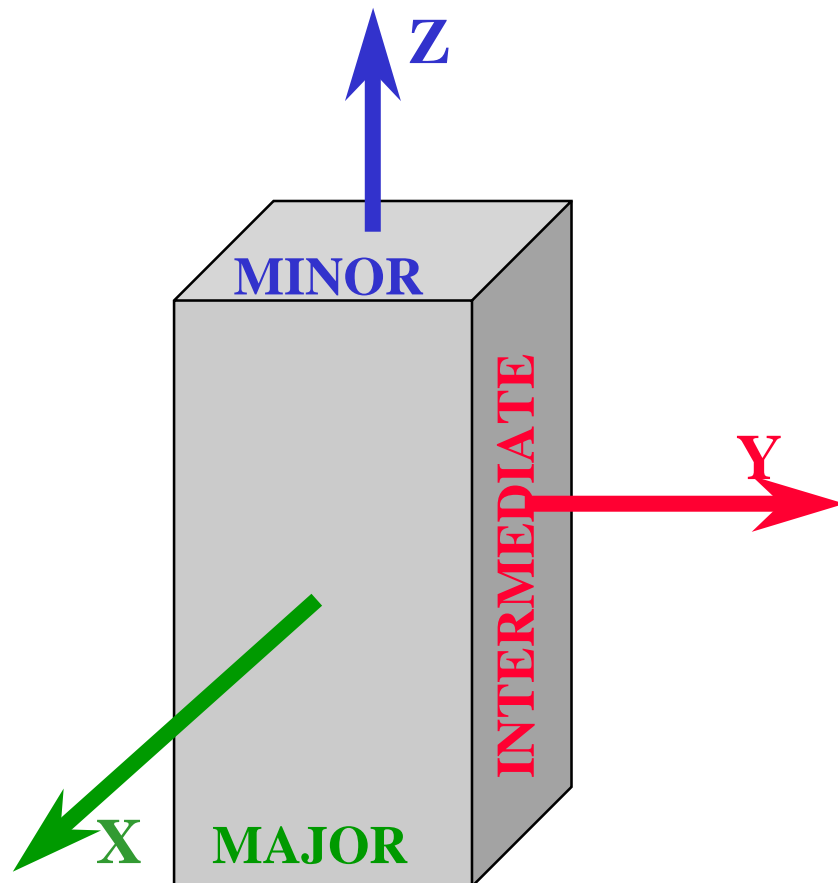
- And when expressed in a **principal** reference frame, it becomes

$$\dot{\omega}_1 = \frac{I_2 - I_3}{I_1} \omega_2 \omega_3 + \frac{g_1}{I_1}$$

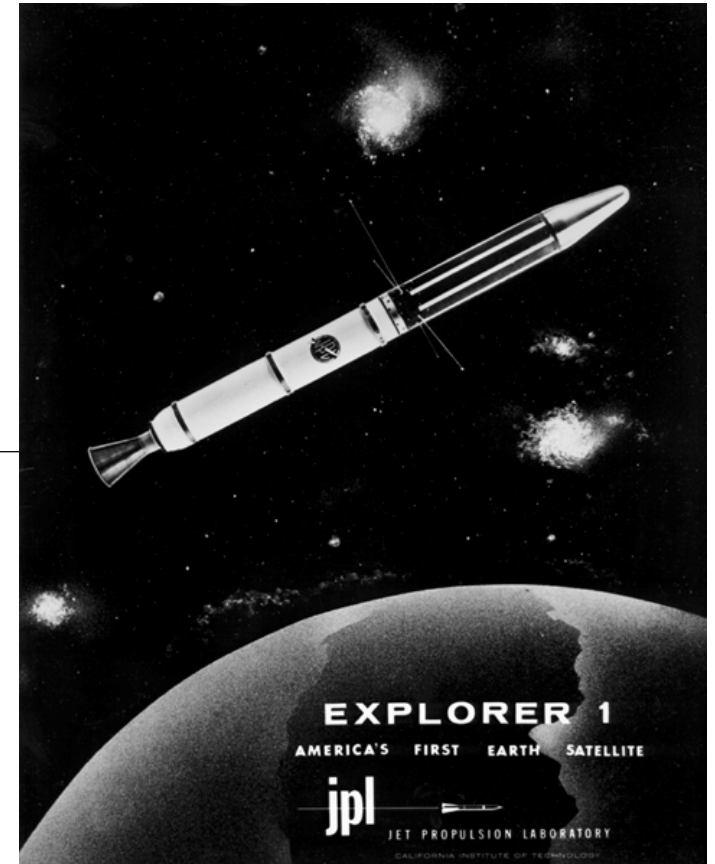
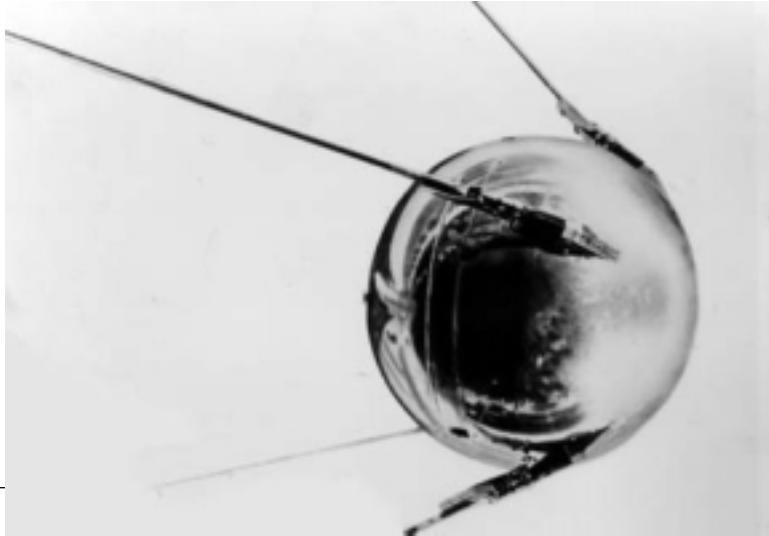
$$\dot{\omega}_2 = \frac{I_3 - I_1}{I_2} \omega_1 \omega_3 + \frac{g_2}{I_2}$$

$$\dot{\omega}_3 = \frac{I_1 - I_2}{I_3} \omega_1 \omega_2 + \frac{g_3}{I_3}$$

Rigid Body Spin Stability

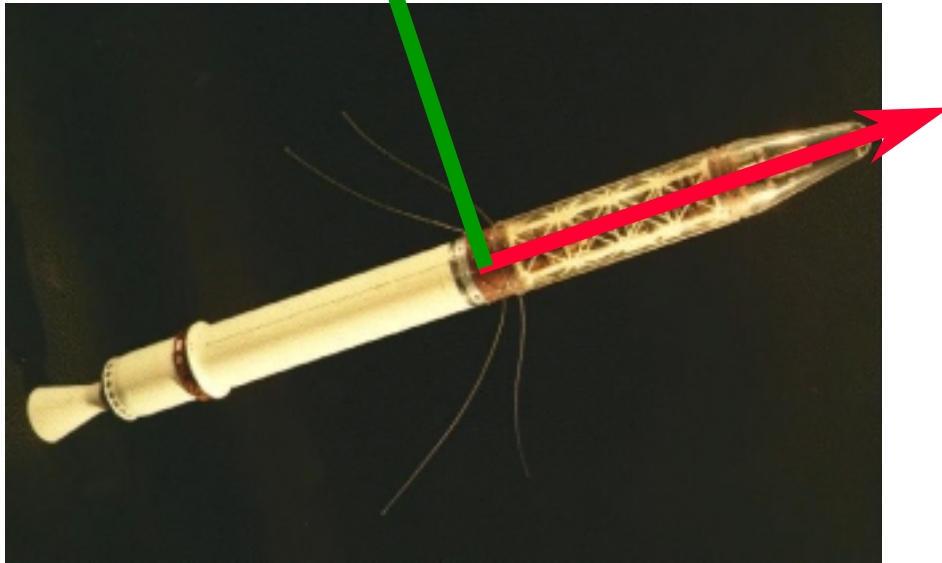


- $I_{xx} > I_{yy} > I_{zz}$
- Major axis spin is stable
- Minor axis spin is stable
- Intermediate axis spin is unstable
- Energy dissipation changes these results
 - Minor axis spin becomes unstable
- This is called the Major-Axis Rule

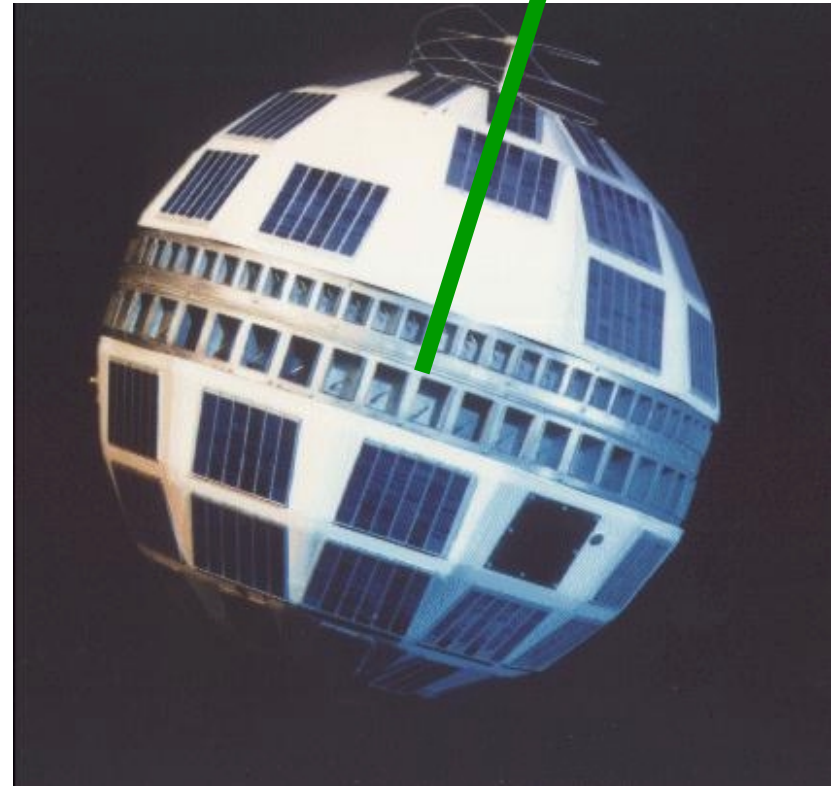


- Sputnik was launched in 1957
- Professor Ronald Bracewell, a radio astronomer at Stanford, deduced that Sputnik was spinning about a symmetry axis, and that it must be the major axis
- He called JPL to make sure that the Explorer I design was taking this into account, but security prevented him from getting through
- Explorer I was designed as a minor axis spinner, launched in 1958

Spin-Stabilized Satellites



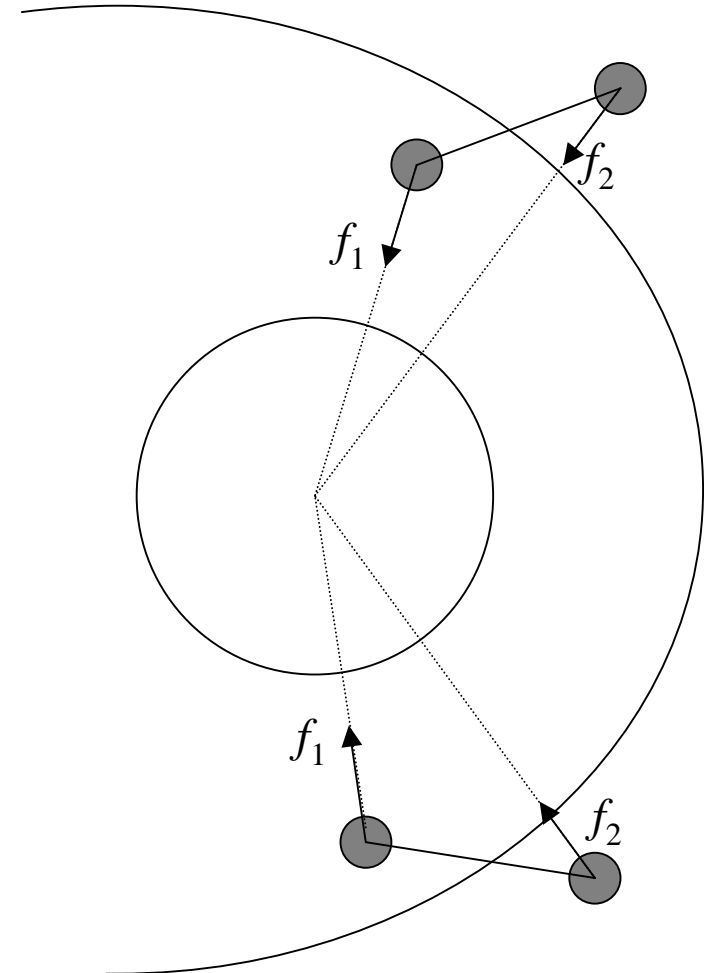
Explorer I (1958) was supposed to be spin-stabilized about its minor axis. It went into a flat spin due to energy dissipation.



Telstar I (1962) was spin-stabilized about its major axis, spinning at about 200 RPM.

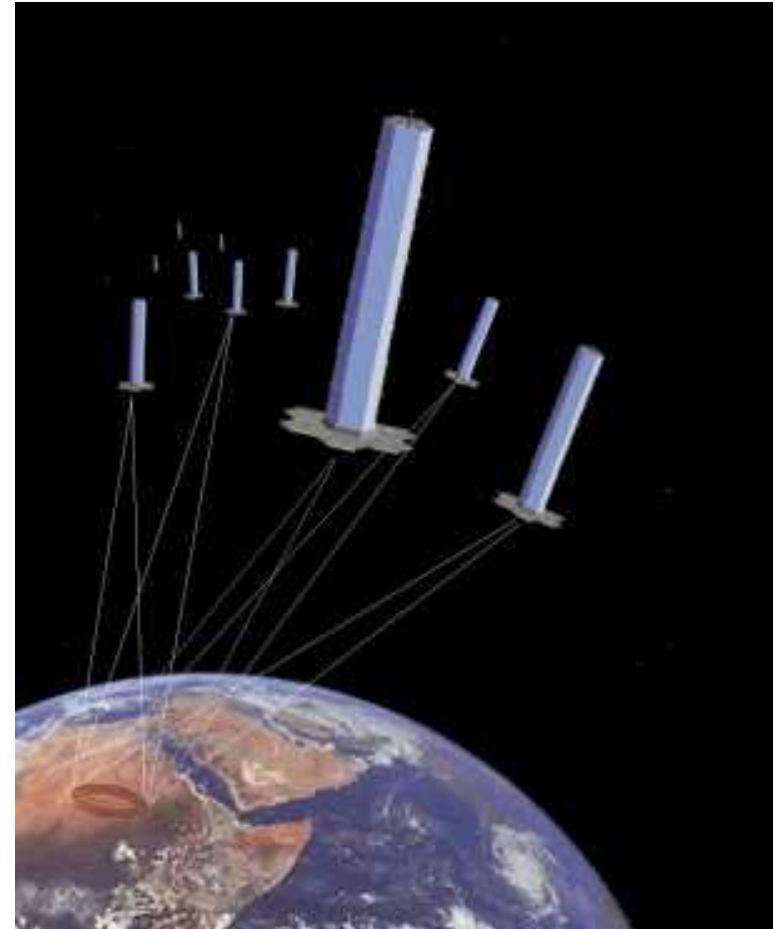
Gravity-Gradient Stabilization

- Gravitational attraction:
$$f = \mu m / r^2$$
- Top: $f_1 > f_2 \Rightarrow$ torque is out of the page
- Bottom: $f_1 > f_2 \Rightarrow$ torque is into the page
- In both cases, the torque is a *restoring* torque, tending to make the satellite swing like a pendulum



Gravity-Gradient Stabilization

- In the 60s was viewed as “free” attitude control
- In general, “ G^2 ” is not accurate enough, **spacecraft can even flip over**
- Not really free, because of boom mass
- However, OrbComm and TechSat 21 use gravity gradient with flexible solar panels on an extensible wrapper around the boom
- The Moon is gravity-gradient stabilized; Lagrange (1736-1813) showed this



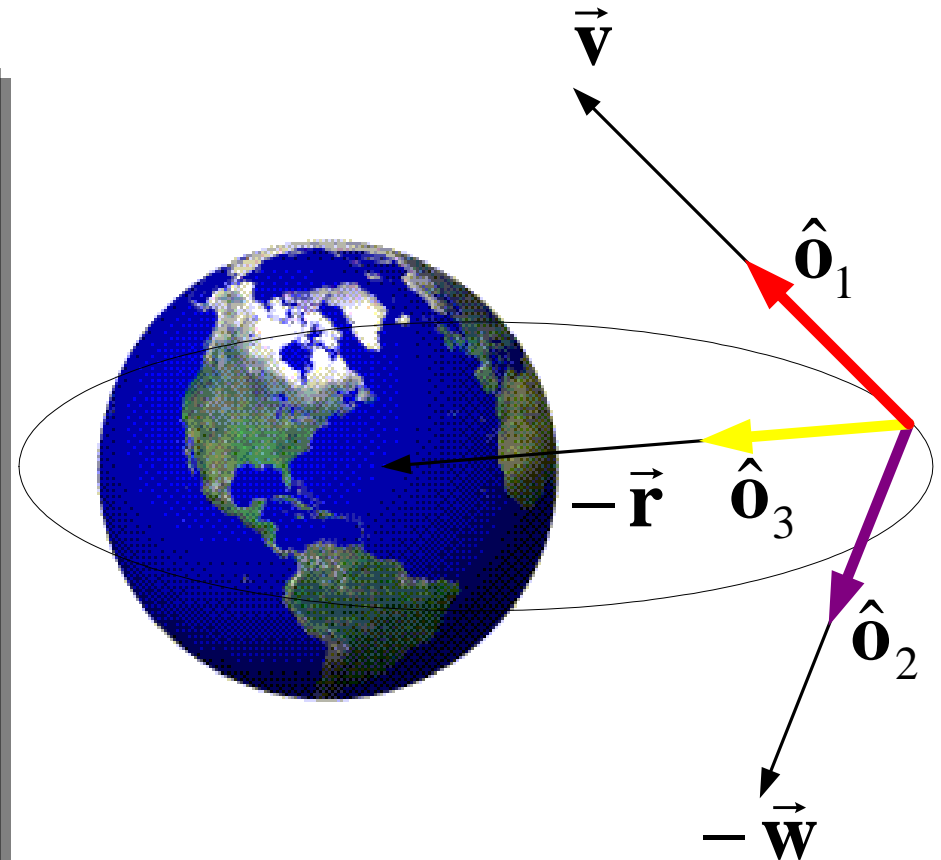
TechSat 21

Augmented G^2 Stabilization

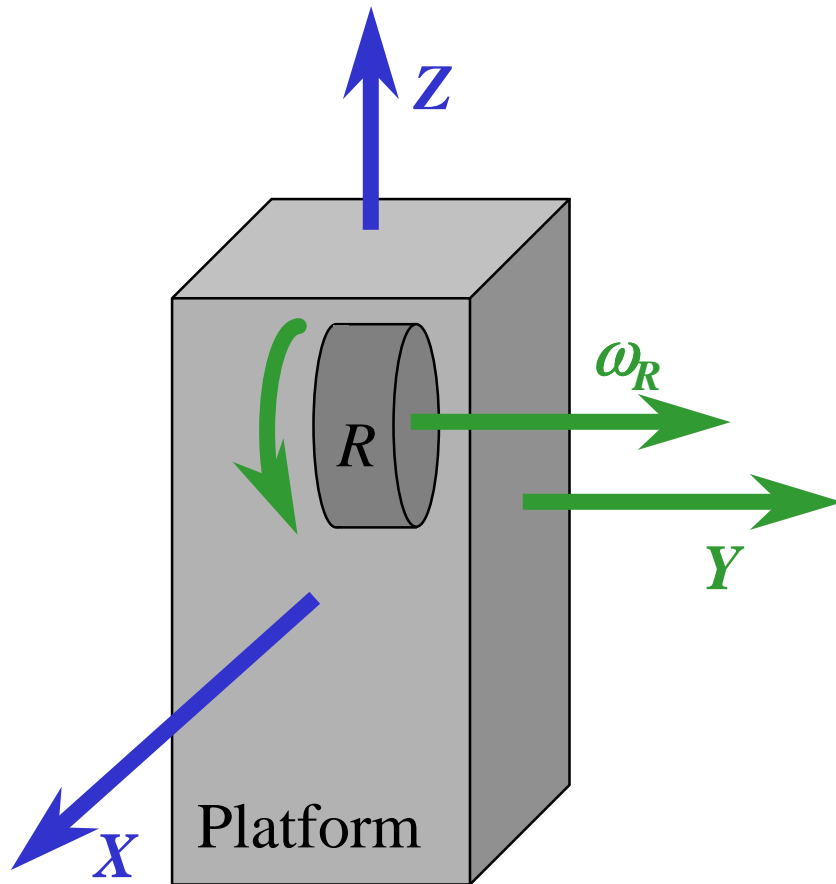
- Problem: with G^2 there is practically no yaw stability
- Solution: Add a small momentum wheel spinning about the pitch axis
- In effect, the wheel is a spin-stabilized s/c, with its angular momentum vector aligned with the orbital angular momentum vector
- Called pitch wheel or yaw wheel
- **Can still flip over!** (Polar Bear)

Roll, Pitch & Yaw

- Same as for aircraft (usually)
- **Roll** is rotation about the velocity vector
- **Pitch** is rotation about the orbit normal vector
- **Yaw** is rotation about the nadir vector
- Keep these color codes in mind



Effect of Rotor on Spin Stability



- A spinning rotor can stabilize the intermediate axis, destabilize others
- Stability condition
$$I_R \omega_R > (I_{xx} - I_{yy}) \omega_y$$
- As with rigid body, energy dissipation changes stability results
→ some stable spins become unstable

Two Spacecraft With Rotors

Defense Support Program



One large rotor
(120 RPM)

Global Positioning System



Four momentum wheels
(several thousand RPM)

Dual-Spin Stabilization

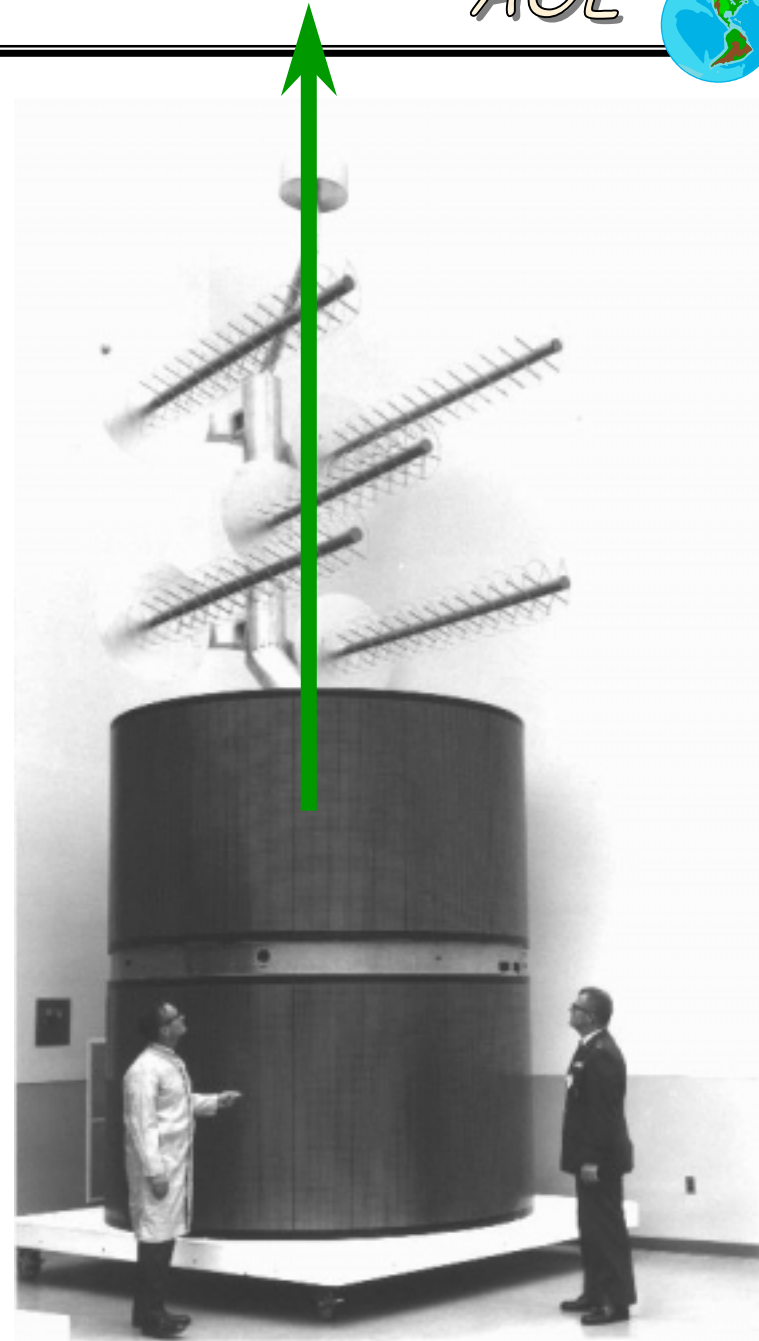
- Spin-stabilized satellites must be major axis spinners: “short and fat”
- Spin axis must in orbit normal direction (well, usually)
- **Two problems:**
 - launch vehicles are “tall and skinny”
 - antennas need to point at earth
- In mid-60s, two engineers invented a **solution**
 - Vernon Landon at RCA
 - Tony Iorillo at Hughes
- Make the spacecraft with **two parts**: one spins relatively fast, the other spins slowly or not at all
- The major axis rule generalizes to make it possible to spin stably about the minor axis
- **Solves both problems:** fits in launch vehicle, points the despun platform at the Earth

Dual-Spin-Stabilized Satellites

TACSAT I (1969) was the first satellite to successfully spin about its minor axis.

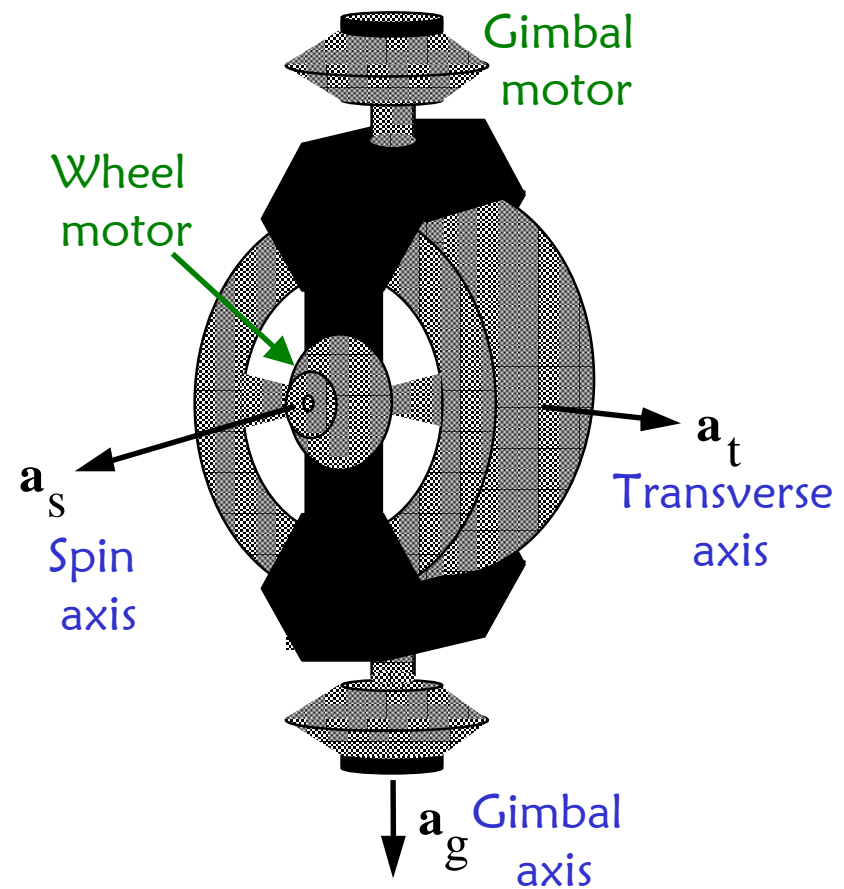
The antenna is the *platform*, and is intended to point continuously at the Earth, spinning at one revolution per orbit.

The cylindrical body is the *rotor*, providing *gyric stability* through its 60 RPM spin.



Gimbaled Momentum Wheels

- Gimbal axis is fixed in the body frame
- Spin axis is controlled by **gimbal motor**
- Spin rate is controlled by **wheel motor**
- Fixed gimbal angle gives *momentum wheel (MW)* or *reaction wheel (RW)*
- Fixed wheel speed gives *control moment gyro (CMG)*



Three-Axis Stabilization

- Instead of keeping the spin axis pointing in a specific direction, keep all 3 axes pointed in specified directions
- Can be done with thrusters, reaction wheels, momentum wheels, control moment gyros, or combination

Magnetic Stabilization

- Spacecraft is moving through Earth's magnetic field \mathbf{B}
- Passing a current through a conductor creates a magnetic moment \mathbf{m} , which in turn causes a torque $\mathbf{g} = \mathbf{m} \times \mathbf{B}$
- Companies make magnetic torquer rods and coils specifically for this ACS application
- There's a simple controller called the \mathbf{B} -dot controller that can spin up or despin a satellite using this torque

Rotational Maneuvers

- Many systems require reorienting the spacecraft from one attitude to another
- Similar to three-axis stabilization, but with additional capability
- Uses thrusters, momentum wheels, reaction wheels, or control moment gyros
- Example: Hubble Space Telescope uses momentum wheels, and turns at about the same speed as a minute hand on a clock

Hubble Pointing

Hubble is the most precisely pointed machine ever devised for astronomy.

Requirement: The telescope must be able to maintain lock on a target for 24 hours without deviating more than $7/1,000$ ths (0.007) of an arc second (2 millionths of a degree) which is about the width of a human hair seen at a distance of a mile.

A laser with the stability and precision of the Hubble, mounted on top of the United States Capitol could hold a steady beam on a dime suspended above New York City, over 200 miles distant. This level of stability and precision is comparable to sinking a hole-in-one on a Los Angeles golf course from a tee in Washington, DC, over 2,000 miles away, in 19 out of 20 attempts.

Course Overview

- Some Mission Analysis concepts
- Kinematics: Vectors, Rotation matrices, Euler angles, Euler parameters (aka quaternions)
- Attitude determination
- Rigid body dynamics (Euler's equations)
- Satellite dynamics applications
- Attitude control